## Resonance interpretation of the

 nonmonotonic behavior in the cross section of $\phi$ photoproduction near thresholdThe 8th International Workshop on the Physics of Excited Nucleons

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## Motivation

- Analysis of differential cross-section (DCS) of phi photoproduction at forward angle by Mibe and Chang, et.al. (Phys. Rev. Lett. 95182001 (2005)) shows the presence of a local peak near threshold ( $E_{\gamma}$ around 2.0 GeV ).
$\longrightarrow$ Seen also by Tedeschi et.al.: unpublished, but shown in some talks.
- We would like to see whether the local peak in the differential cross section (DCS) of $\phi$ photoproduction at forward angle can be explained as a resonance since the conventional model of Pomeron plus $\pi$ and $\eta$ exchanges usually can only give rise to a monotonically-increasing behavior.


## Reaction model

- Here are the tree-level diagrams calculated in our model


(b)

(c)

(d)
- Throughout this presentation,
$-p_{i}$ is the 4 -momentum of the proton in the initial state,
$-k$ is the 4 -momentum of the photon in the initial state,
$-p_{f}$ is the 4 -momentum of the proton in the final state,
$-q$ is the 4 -momentum of the $\phi$ in the final state.


## Pomeron exchange

- We use Donnachie-Landshoff two-gluon exchange model

$$
\begin{gathered}
i \mathcal{M}=i \bar{u}_{f}\left(p_{f}\right) \epsilon_{\phi}^{* \mu} M_{\mu \nu} u_{i}\left(p_{i}\right) \epsilon_{\gamma}^{\nu} \\
M_{\mu \nu}=M(s, t) \Gamma_{\mu \nu}
\end{gathered}
$$

with

$$
\begin{aligned}
M(s, t) & =C_{P} F_{1}(t) F_{2}(t) \frac{1}{s}\left(\frac{s-s_{t h}}{4}\right)^{\alpha_{P}(t)} \exp \left[-i \pi \alpha_{P}(t) / 2\right] \\
\Gamma_{\mu \nu} & =\nLeftarrow\left(g_{\mu \nu}-\frac{q_{\mu} q_{\nu}}{q^{2}}\right)-\gamma_{\nu}\left(k_{\mu}-q_{\mu} \frac{k \cdot q}{q^{2}}\right) \\
& -\left(q_{\nu}-\bar{p}_{\nu} \frac{k \cdot q}{p \cdot k}\right)\left(\gamma_{\mu}-\not q \frac{q_{\mu}}{q^{2}}\right) \quad ; \quad \bar{p}=\frac{1}{2}\left(p_{f}+p_{i}\right)
\end{aligned}
$$

Here, $\Gamma^{\mu \nu}$ is chosen to maintain gauge invariance

- Here

$$
\begin{aligned}
& F_{1}(t)=\frac{4 m_{N}^{2}-2.8 t}{\left(4 m_{N}^{2}-t\right)(1-t / 0.7)^{2}} \\
& F_{2}(t)=\frac{2 \mu_{0}^{2}}{\left(1-t / M_{\phi}^{2}\right)\left(2 \mu_{0}^{2}+M_{\phi}^{2}-t\right)} ; \quad \mu_{0}^{2}=1.1 \mathrm{GeV}^{2}
\end{aligned}
$$

$F_{1}(t)$ is the isoscalar EM form-factor of the nucleon, and $F_{2}(t)$ is the form-factor for the $\phi-\gamma$-Pomeron coupling, and the pomeron trajectory is

$$
\alpha_{P}=1.08+0.25 t
$$

- The strength factor $C_{P}=3.65$ is chosen to fit the total cross sections data at high energy.
- The threshold factor $s_{\text {th }}=1.3 \mathrm{GeV}^{2}$ is chosen to match the forward differential cross sections data at around $E_{\gamma}=6$ GeV.


## $\pi$ and $\eta$ exchanges

- For $t$-channel exchange involving $\pi$ and $\eta$, we use

$$
\begin{aligned}
\mathcal{L}_{\gamma \phi M} & =\frac{e g_{\gamma \phi M}}{m_{\phi}} \epsilon^{\mu \nu \alpha \beta} \partial_{\mu} \phi_{\nu} \partial_{\alpha} A_{\beta} \varphi_{M} \\
\mathcal{L}_{M N N} & =\frac{g_{M N N}}{2 M_{N}} \bar{\psi} \gamma^{\mu} \gamma^{5} \psi \partial_{\mu} \varphi_{M}
\end{aligned}
$$

with $M=(\pi, \eta)$.

- We choose $g_{\pi N N}=13.26, g_{\eta N N}=1.12, g_{\gamma \phi \pi}=-0.14$, and $g_{\gamma \phi \eta}=-0.71$.
- Form factor at each vertex in the $t$-channel diagram is

$$
F_{M N N}(t)=F_{\gamma \phi M}(t)=\frac{\Lambda_{M}^{2}-m_{M}^{2}}{\Lambda_{M}^{2}-t}
$$

- The value $\Lambda_{M}=1.2$ is taken for both $M=(\pi, \eta)$.


## Resonances

- Only spin $1 / 2$ or $3 / 2$ because the resonance is close to the threshold.
- Lagrangian densities that couple spin-1/2 and 3/2 particles to $\gamma N$ or $\phi N$ channels are
$\mathcal{L}_{\phi N N^{*}}^{1 / 2^{ \pm}}=g_{\phi N N^{*}}^{(1)} \bar{\psi}_{N} \Gamma^{ \pm} \gamma^{\mu} \psi_{N^{*}} \phi_{\mu}+g_{\phi N N^{*}}^{(2)} \bar{\psi}_{N} \Gamma^{ \pm} \sigma_{\mu \nu} G^{\mu \nu} \psi_{N^{*}}$,
$\mathcal{L}_{\phi N N^{*}}^{3 / 2^{ \pm}}=i g_{\phi N N^{*}}^{(1)} \bar{\psi}_{N} \Gamma^{ \pm}\left(\partial^{\mu} \psi_{N^{*}}^{\nu}\right) \tilde{G}_{\mu \nu}+g_{\phi N N^{*}}^{(2)} \bar{\psi}_{N} \Gamma^{ \pm} \gamma^{5}\left(\partial^{\mu} \psi_{N^{*}}^{\nu}\right) G_{\mu \nu}$

$$
+i g_{\phi N N^{*}}^{(3)} \bar{\psi}_{N} \Gamma^{ \pm} \gamma^{5} \gamma_{\alpha}\left(\partial^{\alpha} \psi_{N^{*}}^{\nu}-\partial^{\nu} \psi_{N^{*}}^{\alpha}\right)\left(\partial^{\mu} G_{\mu \nu}\right),
$$

where $G_{\mu \nu}=\partial_{\mu} \phi_{\nu}-\partial_{\nu} \phi_{\mu}$ and $\tilde{G}_{\mu \nu}=\frac{1}{2} \epsilon_{\mu \nu \alpha \beta} G^{\alpha \beta}$. The operator $\Gamma^{ \pm}$are given by $\Gamma^{+}=1$ and $\Gamma^{-}=\gamma_{5}$, depending on the parity of the resonance $N^{*}$.

- For the $\gamma N N^{*}$ vertices, simply change $g_{\phi N N^{*}} \rightarrow e g_{\gamma N N^{*}}$ and $\phi_{\mu} \rightarrow A_{\mu}$.
- Current conservation fixes $g_{\gamma N N^{*}}^{(1)} \rightarrow 0$ for $J^{P}=1 / 2^{ \pm}$and the term proportional to $g_{\gamma N N^{*}}^{(3)}$ vanishes in the case of real photon.
- The effect of the width is taken into account in a BreitWigner form by replacing the usual denominator $p^{2}-M_{N^{*}}^{2} \rightarrow$ $p^{2}-M_{N^{*}}^{2}+i M_{N^{*}} \Gamma_{N^{*}}$.
- The form factor for the vertices used in the $s$ - and $u$ channel diagrams is

$$
\begin{equation*}
F_{N^{*}}\left(p^{2}\right)=\frac{\Lambda^{4}}{\Lambda^{4}+\left(p^{2}-M_{N^{*}}^{2}\right)^{2}} \tag{1}
\end{equation*}
$$

with $\Lambda=1.2 \mathrm{GeV}$ for all resonances.

## Fitting to experimental data

- We include only one resonance at a time.
- We fit only masses, widths, and coupling constants of the resonances to the experimental data, while other parameters are fixed during fitting.
- Experimental data to fit
- Differential cross sections (DCS) at forward angle (LEPS 2005)
- DCS as a function of $t$ at eight incoming photon energy bins (LEPS 2005)
- Nine spin-density matrix elements (SDME) at three incoming photon energy bins (New LEPS 2010)
- In our previous work [PLB 691 (2010) 214-218], instead of the new 2010 SDME data, we used five decay angular distributions of $K^{+} K^{-}$pair at two incoming photon energy bins.
- Note that decay angular distributions are functions of SDME.


## Results

- Both $J^{P}=1 / 2^{ \pm}$resonances cannot fit the data.
- DCS at forward angle and as a function of $t$ are markedly improved by the inclusion of the $J^{P}=3 / 2^{ \pm}$resonances.
- In general, SDME are also improved by both $J^{P}=3 / 2^{ \pm}$ resonances.


## DCS at forward angle



Black $\rightarrow J^{P}=3 / 2^{-} \operatorname{Red} \rightarrow J^{P}=3 / 2^{+}$
Full $\rightarrow$ total, Nonresonant $\rightarrow$ dotted, Resonant $\rightarrow$ dashed

## DCS as a function of $t$



Black $\rightarrow J^{P}=3 / 2^{-} \operatorname{Red} \rightarrow J^{P}=3 / 2^{+}$
Full $\rightarrow$ total, Nonresonant $\rightarrow$ dotted, Resonant $\rightarrow$ dashed

## SDME as a function of $t$

$1.77<\mathrm{E}_{\gamma}<1.97 \mathrm{GeV}$


## SDME as a function of $t$

$$
1.97<\mathrm{E}_{\gamma}<2.17 \mathrm{GeV}
$$



## SDME as a function of $t$

$$
2.17<\mathrm{E}_{\gamma}<2.37 \mathrm{GeV}
$$



|  | $J^{P}=3 / 2^{+}$ |  | $J^{P}=3 / 2^{-}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | This work | Previous work | This work | Previous work |
| $M_{N^{*}}(\mathrm{GeV})$ | $2.08 \pm 0.032$ | $2.05 \pm 0.06$ | $2.08 \pm 0.048$ | $2.10 \pm 0.03$ |
| $\Gamma_{N^{*}}(\mathrm{GeV})$ | $0.501 \pm 0.111$ | $0.450 \pm 0.111$ | $0.570 \pm 0.169$ | $0.465 \pm 0.141$ |
| $e g_{\gamma N N^{*}}^{(1)} g_{\phi N N^{*}}^{(1)}$ | $0.003 \pm 0.009$ | $0.000 \pm 0.008$ | $-0.205 \pm 0.095$ | $-0.186 \pm 0.079$ |
| $e g_{\gamma N N^{*}}^{(1)} g_{\phi N N^{*}}^{(2)}$ | $-0.084 \pm 0.057$ | $-0.410 \pm 0.185$ | $-0.025 \pm 0.017$ | $-0.015 \pm 0.030$ |
| $e g_{\gamma N N^{*}}^{(1)} g_{\phi N N^{*}}^{(3)}$ | $0.025 \pm 0.071$ | $-0.318 \pm 0.156$ | $-0.033 \pm 0.018$ | $-0.02 \pm 0.032$ |
| $e g_{\gamma N N^{*}}^{(2)} g_{\phi N N^{*}}^{(1)}$ | 0.002 | $0.000 \pm 0.002$ | -0.266 | $-0.212 \pm 0.076$ |
| $e g_{\gamma N N^{*}}^{(2)} g_{\phi N N^{*}}^{(2)}$ | -0.048 | $-0.100 \pm 0.037$ | -0.033 | $-0.017 \pm 0.035$ |
| $e g_{\gamma N N^{*}}^{(2)} g_{\phi N N^{*}}^{(3)}$ | 0.014 | $-0.078 \pm 0.031$ | -0.043 | $-0.025 \pm 0.037$ |
| $\chi^{2} / N$ | 0.955 | 1.066 | 0.881 | 0.983 |

- The ratio $A_{1 / 2} / A_{3 / 2}=1.05$ (previous work 1.16) for the $J^{P}=$ $3 / 2^{-}$resonance.
- The ratio $A_{1 / 2} / A_{3 / 2}=0.89$ (previous work 0.69 ) for the $J^{P}=$ $3 / 2^{+}$resonance.
- We found that $J^{P}=3 / 2^{-}$resonance parameters are very close to our previous work.
- On the other hand, $J^{P}=3 / 2^{+}$resonance parameters are mostly different, especially the coupling constants.
- We prefer $J^{P}=3 / 2^{-}$based on the stability of the extracted resonance parameters across different sets of experimental data. $\longrightarrow$ cannot be identified with $D_{13}(2080)$ (PDG lists $\left.A_{1 / 2} / A_{3 / 2}=-1.18\right)$


## Effects on $\omega$ photoproduction

- From the $\phi-\omega$ mixing, we expect the resonance to also contribute to $\omega$ photoproduction.
- The coupling constants $g_{\phi N N^{*}}$ and $g_{\omega N N^{*}}$ are related, and in our study we choose to use the so-called "minimal" parametrization,

$$
g_{\phi N N^{*}}=-\tan \Delta \theta_{V} x_{\mathrm{ozi}} g_{\omega N N^{*}}
$$

- By using $x_{\text {ozi }}=12$ for the $J^{P}=3 / 2^{-}$resonance and $x_{\text {ozi }}=9$ for the $J^{P}=3 / 2^{+}$resonance, we found that we can explain quite well the DCS of $\omega$ photoproduction at $W=2.015$ GeV.
- The large value of $x_{\text {ozi }}$ indicates that the resonance has a considerable amount of strangeness content.

DCS of $\omega$ photoproduction as a function of $t$


Data from M. Williams, Phys.Rev.C.80, 065209 (2009)

## Predictions for single polarization observables

$$
\begin{array}{ll}
0.35
\end{array}
$$

## Predictions for double polarization observables

$C_{y x}^{B T}=\frac{d \sigma^{(\theta=-\pi / 4,+x ; U, U)}-d \sigma^{(\theta=-\pi / 4,-x ; U, U)}}{d \sigma^{(\theta=-\pi / 4,+x ; U, U)}+d \sigma^{(\theta=-\pi / 4,-x ; U, U)}}$
$C_{y z}^{B T}=\frac{d \sigma^{(\theta=-\pi / 4,+z ; U, U)}-d \sigma^{(\theta=-\pi / 4,-z ; U, U)}}{d \sigma^{(\theta=-\pi / 4,+z ; U, U)}+d \sigma^{(\theta=-\pi / 4,-z ; U, U)}}$
$C_{z x}^{B T}=\frac{d \sigma^{(+z, \theta=\pi / 2 ; U, U)}-d \sigma^{(+z, \theta=0 ; U, U)}}{d \sigma^{(+z, \theta=\pi / 2 ; U, U)}+d \sigma^{(+z, \theta=0 ; U, U)}}$
$C_{z z}^{B T}=\frac{d \sigma^{(+z,+z ; U, U)}-d \sigma^{(+z,-z ; U, U)}}{d \sigma^{(+z,+z ; U, U)}+d \sigma^{(+z,-z ; U, U)}}$

## Summary and conclusions

- Inclusion of a resonance is needed to explain the nonmonotonic behavior in the DCS of $\phi$-meson photoproduction near threshold.
- Resonance with $J^{P}=3 / 2^{-}$is preferred in this study.
- The resonance seems to have a considerable amount of strangeness content.
- $D_{13}(2080)$ is ruled out based on the different sign of $A_{1 / 2} / A_{3 / 2}$.
- Further experiments, e.g. measurement of single and double polarizations, would be helpful to check our predictions.


## THANK YOU!

